## Finding Probabilities

1. A critical dimension was produced in a particular machining station. Data collected from the samples had Mean = 20.2 ; SD=0.01
a. If 20.222 is USL, what \% is likely to be rejected

b. For a trial batch, you want only components with dimensions between 20.18 \& 20.22. What \% of components are you likely to get?

c. If wish to have $99.9 \%$ acceptable rate from this process, what should be USL?


## Binomial Distribution

2. There is $1 \%$ probability of detecting an error in a transaction by the checker (inspector) in transaction processing team. Every day 150 transactions are processed.
a. Quality Head wants to the probability that there will be any errors in a given day?

## Probability Density Function

Binomial with $\mathrm{n}=150$ and $\mathrm{p}=0.01$

| $x$ | $P(X=x)$ |
| :--- | :--- |
| 0 | 0.221452 |

Probability of Any Errors = 1 - Probability(No errors)

$$
=1-0.221452=0.77855
$$

b. What is the probability of 2 or more errors in a given day?

## Cumulative Distribution Function

$$
\text { Binomial with } \mathrm{n}=150 \text { and } \mathrm{p}=0.01
$$

| $x$ | $P(X \leq x)$ |
| :--- | :--- |
| 1 | 0.556985 |

## Identifying Distributions

3. The data for installation of broad band services at customer location is collected. Based on the data, identify the respective distribution for each of the parameter. (Source:
Distribution_Telecom data_Practicefile)

| Installation TAT in <br> Hours | 3 Parameter Weibull |
| :---: | :--- |
| Commission to SA | 3 Parameter Weibull |
| No. of installations <br> requests in queue | 3 Parameter Weibull |
| Prcessing Time@ <br> Back Office | Normal (Visual Fit) |
| Distance from the <br> SA office | Logistic |
| Distance travelled | Logistic |
| Installation Time by <br> SA | 3 Parameter Weibull |

## Poisson Distribution

4. The "No of installations in queue" is measured hourly (so every data point is per hour data) in attached file. (Source: Distribution_Telecom data_Practicefile). What is the probability that there will be 17 installations in queue in any given hour?

## Probability Density Function

Poisson with mean $=10.256$

| $x$ | $P(X=x)$ |
| ---: | ---: |
| 17 | 0.0151857 |

a. What is the probability that there will be just 3 installations in queue?

## Probability Density Function

Poisson with mean $=10.256$

$$
\begin{array}{lr}
x & P(X=x) \\
\hline 3 & 0.0063191
\end{array}
$$

b. If you were to create capacity of the downstream process based on the number of installations in queue, at $95 \%$ how many installations should be serviced by downstream process to attain nearly a single piece flow (no waiting)?

For 17, the probability is greater than $96.7 \%$. At $95 \%$, the capacity is a decimal as this is a discrete distribution. Hence 17 is the answer.


